

a = 10; c = 1; l = -2; k = .4; m = .3; n = .3;

B = {{l, k, m}, {k, l, n}, {m, n, l}};

B // MatrixForm

$\begin{pmatrix} -2 & 0.4 & 0.3 \\ 0.4 & -2 & 0.3 \\ 0.3 & 0.3 & -2 \end{pmatrix}$

a L k=0.4 m,n  
 $q_i = 10 - 2p_i + 0.3p_2 + 0.3p_3 + 0.3p_4$   
 ~~$+ 0.3p_5 + 0.3p_6$~~

OC = {{1, 0, 0}, {0, 1, 0}, {0, 0, 1}};  
OM = {{1, 1, 1}, {1, 1, 1}, {1, 1, 1}};  
O12 = {{1, 1, 0}, {1, 1, 0}, {0, 0, 1}};  
O13 = {{1, 0, 1}, {0, 1, 0}, {1, 0, 1}};  
O23 = {{1, 0, 0}, {0, 1, 1}, {0, 1, 1}};

Ownership matrices

p = {p1, p2, p3};

q = a + p.B;

pi = (p - c) q;

← *Rangenfunktion*  $q = a + lp_1 + \dots$

FOCC = (p - c) . (B \* OC) + q;

← *Profit*

FOCM = (p - c) . (B \* OM) + q;

FOC12 = (p - c) . (B \* O12) + q;

First Order Conditions for Different Ownerships

FOC13 = (p - c) . (B \* O13) + q;

FOC23 = (p - c) . (B \* O23) + q;

pstC = p /. Solve[{FOCC[[1]] == 0, FOCC[[2]] == 0, FOCC[[3]] == 0}, {p1, p2, p3}];

pstM = p /. Solve[{FOCM[[1]] == 0, FOCM[[2]] == 0, FOCM[[3]] == 0}, {p1, p2, p3}];

pst12 = p /. Solve[{FOC12[[1]] == 0, FOC12[[2]] == 0, FOC12[[3]] == 0}, {p1, p2, p3}];

pst13 = p /. Solve[{FOC13[[1]] == 0, FOC13[[2]] == 0, FOC13[[3]] == 0}, {p1, p2, p3}];

pst23 = p /. Solve[{FOC23[[1]] == 0, FOC23[[2]] == 0, FOC23[[3]] == 0}, {p1, p2, p3}];

↑ *Solve System*

qstC = a + pstC.B;

qstM = a + pstM.B;

qst12 = a + pst12.B;

qst13 = a + pst13.B;

qst23 = a + pst23.B;

pistC = (pstC - c) qstC;

pistM = (pstM - c) qstM;

pist12 = (pst12 - c) qst12;

pist13 = (pst13 - c) qst13;

pist23 = (pst23 - c) qst23;

{pstC, pstM, pst12, pst13, pst23}

{{{3.62869, 3.62869, 3.5443}},  
{4.30795, 4.30795, 4.14238}}, {{3.96197, 3.96197, 3.59429}},  
{3.85878, 3.6693, 3.77902}}, {{3.6693, 3.85878, 3.77902}}}

{qstC, qstM, qst12, qst13, qst23}

{{{5.25738, 5.25738, 5.08861}}, {{4.35, 4.35, 4.3}}, {{4.73914, 4.73914, 5.18859}},  
{4.88386, 5.33861, 4.7004}}, {{5.33861, 4.88386, 4.7004}}}

{pistC, pistM, pist12, pist13, pist23}

{{{13.82, 13.82, 12.947}}, {{14.3896, 14.3896, 13.5123}}, {{14.0372, 14.0372, 13.4607}},  
{13.9619, 14.2504, 13.0625}}, {{14.2504, 13.9619, 13.0625}}}